

THREE DIMENSIONAL GEOMETRY PYQ

1. The distance of the point $(1, -5, 9)$ from the plane $x - y + z = 5$ measured along a straight line $x = y = z$ is : **[AIEEE-2011]**
- (1) $3\sqrt{5}$ (2) $10\sqrt{3}$
 (3) $5\sqrt{3}$ (4) $3\sqrt{10}$
2. An equation of a plane parallel to the plane $x - 2y + 2z - 5 = 0$ and at a unit distance from the origin is : **[AIEEE-2012]**
- (1) $x - 2y + 2z + 5 = 0$
 (2) $x - 2y + 2z - 3 = 0$
 (3) $x - 2y + 2z + 1 = 0$
 (4) $x - 2y + 2z - 1 = 0$
3. If the lines $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-1}{4}$ and $\frac{x-3}{1} = \frac{y-k}{2} = \frac{z}{1}$ intersect, then k is equal to: **[AIEEE-2012]**
- (1) 0 (2) -1 (3) $\frac{2}{9}$ (4) $\frac{9}{2}$
4. The equation of a plane containing the line $\frac{x+1}{-3} = \frac{y-3}{2} = \frac{z+2}{1}$ and the point $(0, 7, -7)$ is: **[AIEEE-2012 (Online)]**
- (1) $x + 2y - z = 21$
 (2) $x + y + z = 0$
 (3) $3x - 2y + 3z + 35 = 0$
 (4) $3x + 2y + 5z + 21 = 0$
5. Consider the following planes :
 $P : x + y - 2z + 7 = 0$
 $Q : x + y + 2z + 2 = 0$
 $R : 3x + 3y - 6z - 11 = 0$ **[AIEEE-2012 (Online)]**
- (1) P and R are perpendicular
 (2) P and Q are parallel
 (3) P and R are parallel
 (4) Q and R are perpendicular
6. The distance of the point $-\hat{i} + 2\hat{j} + 6\hat{k}$ from the straight line that passes through the point $2\hat{i} + 3\hat{j} - 4\hat{k}$ and is parallel to the vector $6\hat{i} + 3\hat{j} - 4\hat{k}$ is : **[AIEEE-2012 (Online)]**
- (1) 8 (2) 7
 (3) 10 (4) 9
7. A line with positive direction cosines passes through the point $P(2, -1, 2)$ and makes equal angles with the coordinate axes. If the line meets the plane $2x + y + z = 9$ at point Q, then the length PQ equals **[AIEEE-2012 (Online)]**
- (1) 2 (2) $\sqrt{3}$
 (3) 1 (4) $\sqrt{2}$
8. The values of a for which the two points $(1, a, 1)$ and $(-3, 0, a)$ lie on the opposite sides of the plane $3x + 4y - 12z + 13 = 0$, satisfy :- **[AIEEE-2012 (Online)]**
- (1) $0 < a < 1/3$
 (2) $a = 0$
 (3) $-1 < a < 0$
 (4) $a < -1$ or $a > 1/3$
9. If the three planes $x = 5$, $2x - 5ay + 3z - 2 = 0$ and $3bx + y - 3z = 0$ contain a common line, then (a, b) is equal to :- **[AIEEE-2012 (Online)]**
- (1) $\left(-\frac{1}{5}, \frac{8}{15}\right)$ (2) $\left(-\frac{8}{15}, \frac{1}{5}\right)$
 (3) $\left(\frac{1}{5}, -\frac{8}{15}\right)$ (4) $\left(\frac{8}{15}, -\frac{1}{5}\right)$
10. The coordinates of the foot of perpendicular from the point $(1, 0, 0)$ to the line $\frac{x-1}{2} = \frac{y+1}{-3} = \frac{z+10}{8}$ are :- **[AIEEE-2012 (Online)]**
- (1) $(5, -8, -4)$ (2) $(2, -3, 8)$
 (3) $(3, -4, -2)$ (4) $(1, -1, -10)$

11. Distance between two parallel planes $2x + y + 2z = 8$ and $4x + 2y + 4z + 5 = 0$ is :-

[JEE (Main)-2013]

(1) $\frac{3}{2}$ (2) $\frac{5}{2}$

(3) $\frac{7}{2}$ (4) $\frac{9}{2}$

12. If the lines $\frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{-k}$ and

$\frac{x-1}{k} = \frac{y-4}{2} = \frac{z-5}{1}$ are coplanar, then k can

have : [JEE (Main)-2013]

- (1) any value
- (2) exactly one value
- (3) exactly two values
- (4) exactly three values.

13. The image of the line

$\frac{x-1}{3} = \frac{y-3}{1} = \frac{z-4}{-5}$ in the plane

$2x - y + z + 3 = 0$ is the line : [JEE (Main)-2014]

(1) $\frac{x+3}{3} = \frac{y-5}{1} = \frac{z-2}{-5}$

(2) $\frac{x+3}{-3} = \frac{y-5}{-1} = \frac{z+2}{5}$

(3) $\frac{x-3}{3} = \frac{y+5}{1} = \frac{z-2}{-5}$

(4) $\frac{x-3}{-3} = \frac{y+5}{-1} = \frac{z-2}{5}$

14. The angle between the lines whose direction cosines satisfy the equations $l + m + n = 0$ and $l^2 = m^2 + n^2$ is : [JEE (Main)-2014]

(1) $\frac{\pi}{3}$ (2) $\frac{\pi}{4}$

(3) $\frac{\pi}{6}$ (4) $\frac{\pi}{2}$

15. The equation of the plane containing the line $2x - 5y + z = 3$; $x + y + 4z = 5$, and parallel to the plane, $x + 3y + 6z = 1$, is

(1) $x + 3y + 6z = 7$ [JEE (Main)-2015]

(2) $2x + 6y + 12z = -13$

(3) $2x + 6y + 12z = 13$

(4) $x + 3y + 6z = -7$

16. The distance of the point (1, 0, 2) from the point

of intersection of the line $\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{12}$

and the plane $x - y + z = 16$, is :

[JEE (Main)-2015]

(1) $3\sqrt{21}$ (2) 13

(3) $2\sqrt{14}$ (4) 8

17. The distance of the point (1, -5, 9) from the plane $x - y + z = 5$ measured along the line $x = y = z$ is : [JEE (Main)-2016]

(1) $\frac{20}{3}$ (2) $3\sqrt{10}$

(3) $10\sqrt{3}$ (4) $\frac{10}{\sqrt{3}}$

18. If the line, $\frac{x-3}{2} = \frac{y+2}{-1} = \frac{z+4}{3}$ lies in the plane, $lx + my - z = 9$, then $l^2 + m^2$ is equal to :-

[JEE (Main)-2016]

(1) 2 (2) 26

(3) 18 (4) 5

19. If the image of the point P(1, -2, 3) in the plane, $2x + 3y - 4z + 22 = 0$ measured parallel to line,

$\frac{x}{1} = \frac{y}{4} = \frac{z}{5}$ is Q, then PQ is equal to :-

[JEE (Main)-2017]

(1) $6\sqrt{5}$ (2) $3\sqrt{5}$

(3) $2\sqrt{42}$ (4) $\sqrt{42}$

20. The distance of the point (1, 3, -7) from the plane passing through the point (1, -1, -1), having normal perpendicular to both the lines $\frac{x-1}{1} = \frac{y+2}{-2} = \frac{z-4}{3}$

and $\frac{x-2}{2} = \frac{y+1}{-1} = \frac{z+7}{-1}$, is :- **[JEE (Main)-2017]**

- (1) $\frac{10}{\sqrt{74}}$ (2) $\frac{20}{\sqrt{74}}$ (3) $\frac{10}{\sqrt{83}}$ (4) $\frac{5}{\sqrt{83}}$

21. The length of the projection of the line segment joining the points (5, -1, 4) and (4, -1, 3) on the plane, $x + y + z = 7$ is : **[JEE (Main)-2018]**

- (1) $\frac{2}{3}$ (2) $\frac{1}{3}$ (3) $\frac{\sqrt{2}}{3}$ (4) $\frac{2}{\sqrt{3}}$

22. If L_1 is the line of intersection of the planes $2x - 2y + 3z - 2 = 0$, $x - y + z + 1 = 0$ and L_2 is the line of intersection of the planes $x + 2y - z - 3 = 0$, $3x - y + 2z - 1 = 0$, then the distance of the origin from the plane, containing the lines L_1 and L_2 is : **[JEE (Main)-2018]**

- (1) $\frac{1}{3\sqrt{2}}$ (2) $\frac{1}{2\sqrt{2}}$ (3) $\frac{1}{\sqrt{2}}$ (4) $\frac{1}{4\sqrt{2}}$

23. The point P is the intersection of the straight line joining the points Q(2,3,5) and R(1,-1,4) with the plane $5x - 4y - z = 1$. If S is the foot of the perpendicular drawn from the point T(2,1,4) to QR, then the length of the line segment PS is -

[IIT-2012]

- (1) $\frac{1}{\sqrt{2}}$ (2) $\sqrt{2}$ (3) 2 (4) $2\sqrt{2}$

24. The equation of a plane passing through the line of intersection of the planes $x + 2y + 3z = 2$ and

$x - y + z = 3$ and at a distance $\frac{2}{\sqrt{3}}$ from the point

(3, 1, -1) is **[IIT-2012]**

(1) $5x - 11y + z = 17$ (2) $\sqrt{2}x + y = 3\sqrt{2} - 1$

(3) $x + y + z = \sqrt{3}$ (4) $x - \sqrt{2}y = 1 - \sqrt{2}$

*25. If the straight lines $\frac{x-1}{2} = \frac{y+1}{k} = \frac{z}{2}$ and

$\frac{x+1}{5} = \frac{y+1}{2} = \frac{z}{k}$ are coplanar, then the plane(s)

containing these two lines is(are) **[IIT-2012]**

(1) $y + 2z = -1$

(2) $y + z = -1$

(3) $y - z = -1$

(4) $y - 2z = -1$

26. Perpendiculars are drawn from points on the line

$\frac{x+2}{2} = \frac{y+1}{-1} = \frac{z}{3}$ to the plane $x + y + z = 3$. The

feet of perpendiculars lie on the line

[JEE-Advanced 2013]

(1) $\frac{x}{5} = \frac{y-1}{8} = \frac{z-2}{-13}$

(2) $\frac{x}{2} = \frac{y-1}{3} = \frac{z-2}{-5}$

(3) $\frac{x}{4} = \frac{y-1}{3} = \frac{z-2}{-7}$

(4) $\frac{x}{2} = \frac{y-1}{-7} = \frac{z-2}{5}$

*27. A line ℓ passing through the origin is perpendicular to the lines

$\ell_1 : (3+t)\hat{i} + (-1+2t)\hat{j} + (4+2t)\hat{k}, -\infty < t < \infty$

$\ell_2 : (3+2s)\hat{i} + (3+2s)\hat{j} + (2+s)\hat{k}, -\infty < s < \infty$

Then, the coordinate(s) of the point(s) on ℓ_2 at a distance of $\sqrt{17}$ from the point of intersection of ℓ and ℓ_1 is(are) - **[JEE-Advanced 2013]**

(1) $(\frac{7}{3}, \frac{7}{3}, \frac{5}{3})$ (2) (-1, -1, 0)

(3) (1, 1, 1) (4) $(\frac{7}{9}, \frac{7}{9}, \frac{8}{9})$

***28.** Two lines $L_1 : x = 5, \frac{y}{3-\alpha} = \frac{z}{-2}$ and

$L_2 : x = \alpha, \frac{y}{-1} = \frac{z}{2-\alpha}$ are coplanar. Then α can

take value(s) [JEE-Advanced 2013]

- (1) 1 (2) 2 (3) 3 (4) 4

29. Consider the lines

$$L_1 : \frac{x-1}{2} = \frac{y}{-1} = \frac{z+3}{1}, L_2 : \frac{x-4}{1} = \frac{y+3}{1} = \frac{z+3}{2}$$

and the planes $P_1 : 7x + y + 2z = 3, P_2 :$

$3x + 5y - 6z = 4$. Let $ax + by + cz = d$ be the equation of the plane passing through the point of intersection of lines L_1 and L_2 and perpendicular to planes P_1 and P_2 .

Match List-I with List-II and select the correct answer using the code given below the lists.

[JEE-Advanced 2013]

List-I	List-II
P. a =	1. 13
Q. b =	2. -3
R. c =	3. 1
S. d =	4. -2

Codes :

	P	Q	R	S
(1)	3	2	4	1
(2)	1	3	4	2
(3)	3	2	1	4
(4)	2	4	1	3

30. From a point $P(\lambda, \lambda, \lambda)$, perpendiculars PQ and PR are drawn respectively on the lines $y = x, z = 1$ and $y = -x, z = -1$. If P is such that $\angle QPR$ is a right angle, then the possible value(s) of λ is(are)

[JEE(Advanced)-2014]

- (1) $\sqrt{2}$ (2) 1 (3) -1 (4) $-\sqrt{2}$

*** Marked Questions are multiple answer**

PREVIOUS YEARS QUESTIONS				ANSWER KEY				Exercise-II			
Que.	1	2	3	4	5	6	7	8	9	10	
Ans.	2	2	4	2	3	2	2	4	3	3	
Que.	11	12	13	14	15	16	17	18	19	20	
Ans.	3	3	1	1	1	2	3	1	3	3	
Que.	21	22	23	24	25	26	27	28	29	30	
Ans.	3	1	1	1	2,3	4	2,4	1,4	1	3	