

AREA UNDER THE CURVE- PYQ

1. The area enclosed between the curves $y^2 = x$ and $y = |x|$ is- **[AIEEE-2007]**
 (1) $\frac{2}{3}$ (2) 1 (3) $\frac{1}{6}$ (4) $\frac{1}{3}$
2. The area of the plane region bounded by the curves $x + 2y^2 = 0$ and $x + 3y^2 = 1$ is equal to- **[AIEEE-2008]**
 (1) $\frac{5}{3}$ (2) $\frac{1}{3}$ (3) $\frac{2}{3}$ (4) $\frac{4}{3}$
3. The area of the region bounded by the parabola $(y - 2)^2 = x - 1$, the tangent to the parabola at the point (2, 3) and the x-axis is :- **[AIEEE-2009]**
 (1) 9 (2) 12 (3) 3 (4) 6
4. The area bounded by the curves $y = \cos x$ and $y = \sin x$ between the ordinates $x = 0$ and $x = \frac{3\pi}{2}$ is :- **[AIEEE-2010]**
 (1) $4\sqrt{2} - 2$ (2) $4\sqrt{2} + 2$
 (3) $4\sqrt{2} - 1$ (4) $4\sqrt{2} + 1$
5. The area of the region enclosed by the curves $y = x$, $x = e$, $y = \frac{1}{x}$ and the positive x-axis is:- **[AIEEE-2011]**
 (1) $\frac{3}{2}$ square units (2) $\frac{5}{2}$ square units
 (3) $\frac{1}{2}$ square units (4) 1 square units
6. The area bounded by the curves $y^2 = 4x$ and $x^2 = 4y$ is : **[AIEEE-2011]**
 (1) 0 (2) $\frac{32}{3}$ (3) $\frac{16}{3}$ (4) $\frac{8}{3}$
7. The area bounded between the parabolas $x^2 = \frac{y}{4}$ and $x^2 = 9y$, and the straight line $y = 2$ is : **[AIEEE-2012]**
 (1) $10\sqrt{2}$ (2) $20\sqrt{2}$ (3) $\frac{10\sqrt{2}}{3}$ (4) $\frac{20\sqrt{2}}{3}$
8. The area (in square units) bounded by the curves $y = \sqrt{x}$, $2y - x + 3 = 0$, x-axis and lying in the first quadrant is : **[JEE(Main)-2013]**
 (1) 9 (2) 36 (3) 18 (4) $\frac{27}{4}$
9. The area bounded by the curve $y = \ln(x)$ and the lines $y = 0$, $y = \ln(3)$ and $x = 0$ is equal to : **[JEE-Main (On line)-2013]**
 (1) $3 \ln(3) - 2$ (2) 3
 (3) 2 (4) $3 \ln(3) + 2$
10. The area of the region (in sq. units), in the first quadrant, bounded by the parabola $y = 9x^2$ and the lines $x = 0$, $y = 1$ and $y = 4$, is :- **[JEE-Main (On line)-2013]**
 (1) $\frac{7}{9}$ (2) $\frac{14}{3}$ (3) $\frac{14}{9}$ (4) $\frac{7}{3}$
11. The area under the curve $y = |\cos x - \sin x|$, $0 \leq x \leq \frac{\pi}{2}$, and above x-axis is : **[JEE-Main (On line)-2013]**
 (1) $2\sqrt{2}$ (2) $2\sqrt{2} + 2$
 (3) 0 (4) $2\sqrt{2} - 2$
12. The area of the region described by $A = \{(x, y) : x^2 + y^2 \leq 1 \text{ and } y^2 \leq 1 - x\}$ is : **[JEE(Main)-2014]**
 (1) $\frac{\pi}{2} + \frac{4}{3}$ (2) $\frac{\pi}{2} - \frac{4}{3}$ (3) $\frac{\pi}{2} - \frac{2}{3}$ (4) $\frac{\pi}{2} + \frac{2}{3}$
13. The area (in sq. units) of the region described by $\{(x, y) : y^2 \leq 2x \text{ and } y \geq 4x - 1\}$ is : **[JEE (Main) 2015]**
 (1) $\frac{15}{64}$ (2) $\frac{9}{32}$ (3) $\frac{7}{32}$ (4) $\frac{5}{64}$
14. The area (in sq. units) of the region $\{(x, y) : y^2 \geq 2x \text{ and } x^2 + y^2 \leq 4x, x \geq 0, y \geq 0\}$ is :- **[JEE(Main)-2016]**
 (1) $\frac{\pi}{2} - \frac{2\sqrt{2}}{3}$ (2) $\pi - \frac{4}{3}$
 (3) $\pi - \frac{8}{3}$ (4) $\pi - \frac{4\sqrt{2}}{3}$
15. The area (in sq. units) of the region $\{(x, y) : x \geq 0, x + y \leq 3, x^2 \leq 4y \text{ and } y \leq 1 + \sqrt{x}\}$ is : **[JEE(Main)-2017]**
 (1) $\frac{5}{2}$ (2) $\frac{59}{12}$ (3) $\frac{3}{2}$ (4) $\frac{7}{3}$
16. Let $g(x) = \cos x^2$, $f(x) = \sqrt{x}$ and α, β ($\alpha < \beta$) be the roots of the quadratic equation $18x^2 - 9\pi x + \pi^2 = 0$. Then the area (in sq. units) bounded by the curve $y = (g \circ f)(x)$ and the lines $x = \alpha$, $x = \beta$ and $y = 0$ is- **[JEE(MAIN)-2018]**
 (1) $\frac{1}{2}(\sqrt{3} + 1)$ (2) $\frac{1}{2}(\sqrt{3} - \sqrt{2})$
 (3) $\frac{1}{2}(\sqrt{2} - 1)$ (4) $\frac{1}{2}(\sqrt{3} - 1)$

17. The area of the region between the curves

$$y = \sqrt{\frac{1 + \sin x}{\cos x}} \text{ and } y = \sqrt{\frac{1 - \sin x}{\cos x}} \text{ bounded by the}$$

lines $x = 0$ and $x = \frac{\pi}{4}$ is- **[IIT-2008]**

(1) $\int_0^{\sqrt{2}-1} \frac{t}{(1+t^2)\sqrt{1-t^2}} dt$ (2) $\int_0^{\sqrt{2}-1} \frac{4t}{(1+t^2)\sqrt{1-t^2}} dt$

(3) $\int_0^{\sqrt{2}+1} \frac{4t}{(1+t^2)\sqrt{1-t^2}} dt$ (4) $\int_0^{\sqrt{2}+1} \frac{t}{(1+t^2)\sqrt{1-t^2}} dt$

*18. Area of the region bounded by the curve $y = e^x$ and lines $x = 0$ and $y = e$ is :- **[IIT-2009]**

(1) $e - 1$ (2) $\int_1^e \ln(e + 1 - y) dy$

(3) $e - \int_0^1 e^x dx$ (4) $\int_1^e \ln y dy$

19. Let the straight line $x = b$ divide the area enclosed by $y = (1 - x)^2$, $y = 0$ and $x = 0$ into two parts $R_1(0 \leq x \leq b)$ and $R_2(b \leq x \leq 1)$ such that

$R_1 - R_2 = \frac{1}{4}$. Then b equals **[IIT-2011]**

(1) $\frac{3}{4}$ (2) $\frac{1}{2}$ (3) $\frac{1}{3}$ (4) $\frac{1}{4}$

20. Let $f: [-1, 2] \rightarrow [0, \infty)$ be a continuous function such that $f(x) = f(1-x)$ for all $x \in [-1, 2]$. Let

$R_1 = \int_{-1}^2 x f(x) dx$, and R_2 be the area of the region

bounded by $y = f(x)$, $x = -1$, $x = 2$, and the x -axis. Then - **[IIT-2011]**

(1) $R_1 = 2R_2$ (2) $R_1 = 3R_2$
 (3) $2R_1 = R_2$ (4) $3R_1 = R_2$

21. The area enclosed by the curve $y = \sin x + \cos x$

and $y = |\cos x - \sin x|$ over the interval $\left[0, \frac{\pi}{2}\right]$

is **[JEE(Adv.)-2013]**

(1) $4(\sqrt{2} - 1)$ (2) $2\sqrt{2}(\sqrt{2} - 1)$
 (3) $2(\sqrt{2} + 1)$ (4) $2\sqrt{2}(\sqrt{2} + 1)$

22. Let $F(x) = \int_x^{x^2 + \frac{\pi}{6}} 2 \cos^2 t dt$ for all $x \in \mathbb{R}$ and

$f: \left[0, \frac{1}{2}\right] \rightarrow [0, \infty)$ be a continuous function. For

$a \in \left[0, \frac{1}{2}\right]$, if $F(a) + 2$ is the area of the region

bounded by $x = 0$, $y = 0$, $y = f(x)$ and $x = a$, then $f(0)$ is **[JEE 2015]**

*23. If the line $x = \alpha$ divides the area of region $R = \{(x, y) \in \mathbb{R}^2 : x^3 \leq y \leq x, 0 \leq x \leq 1\}$ into two equal parts, then **[JEE(Advanced)-2017]**

(1) $\frac{1}{2} < \alpha < 1$ (2) $\alpha^4 + 4\alpha^2 - 1 = 0$

(3) $0 < \alpha \leq \frac{1}{2}$ (4) $2\alpha^4 - 4\alpha^2 + 1 = 0$

*24. Let $f: [0, \infty) \rightarrow \mathbb{R}$ be a continuous function such

that $f(x) = 1 - 2x + \int_0^x e^{-t} f(t) dt$

for all $x \in [0, \infty)$. Then, which of the following statement(s) is (are) TRUE ? **[JEE(Advanced)-2018]**

- (1) The curve $y = f(x)$ passes through the point $(1, 2)$
- (2) The curve $y = f(x)$ passes through the point $(2, -1)$
- (3) The area of the region

$\{(x, y) \in [0, 1] \times \mathbb{R} : f(x) \leq y \leq \sqrt{1-x^2}\}$

is $\frac{\pi - 2}{4}$

- (4) The area of the region

$\{(x, y) \in [0, 1] \times \mathbb{R} : f(x) \leq y \leq \sqrt{1-x^2}\}$

is $\frac{\pi - 1}{4}$

* Marked Questions are multiple answer

| PREVIOUS YEARS QUESTIONS | | | | ANSWER KEY | | | | Exercise-II | | | |
|--------------------------|----|----|-----|------------|----|----|----|-------------|----|----|--|
| Que. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | |
| Ans. | 3 | 4 | 1 | 1 | 1 | 3 | 4 | 1 | 3 | 3 | |
| Que. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | |
| Ans. | 4 | 1 | 2 | 3 | 1 | 4 | 2 | 2,3,4 | 2 | 3 | |
| Que. | 21 | 22 | 23 | 24 | | | | | | | |
| Ans. | 2 | 3 | 1,4 | 2,3 | | | | | | | |