

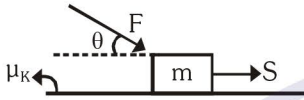
# WORK, POWER AND ENERGY

# EXERCISE

1. A body of mass  $m$  is displaced from point A(3, 1, 2) to point B(4, 2, 1) under the effect of a force  $\vec{F} = (\hat{i} + 2\hat{j} + 3\hat{k})\text{N}$ , calculate W.D. by the force.

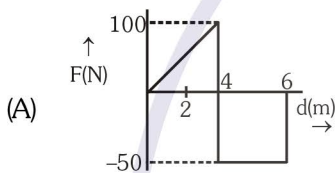
- (1) 57 J    (2) 11 J    (3) 0    (4) 22 J

2. Find work done by friction for displacement 'S' ?

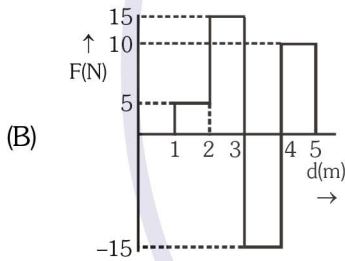


- (1)  $\mu_k(mg + F\sin\theta).S$     (2)  $-\mu_k(mg + F\sin\theta).S$   
 (3)  $\mu_k(mg - F\sin\theta).S$     (4)  $-\mu_k(mg - F\sin\theta).S$

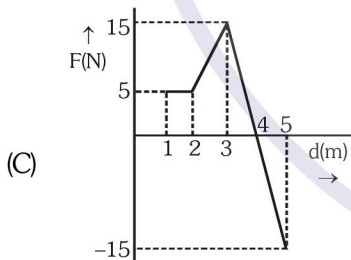
3. Calculate the work done for following F-d curves



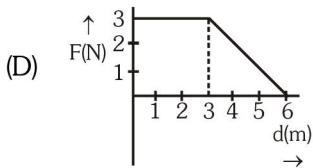
(P) 100 J



(Q) 13.5 J



(R) 15 J



- (1) (A - P); (B - Q); (C - Q); (D - R)  
 (2) (A - P); (B - R); (C - R); (D - Q)  
 (3) (A - P); (B - P); (C - Q); (D - R)  
 (4) (A - P); (B - P); (C - R); (D - Q)

4. A force  $F = Kx^2$  acts on a particle at an angle of  $60^\circ$  with the x-axis. the work done in displacing the particle from  $x_1$  to  $x_2$  will be -

- (1)  $\frac{kx^2}{2}$     (2)  $\frac{k}{2}(x_2^2 - x_1^2)$   
 (3)  $\frac{k}{6}(x_2^3 - x_1^3)$     (4)  $\frac{k}{3}(x_2^3 - x_1^3)$

5. A force acts on a 30 g particle in such a way that the position of the particle as a function of time is given by  $x = 3t - 4t^2 + t^3$ , where  $x$  is in metres and  $t$  is in seconds. The work done during the first 4 second is :-

- (1) 5.28 J    (2) 450 mJ    (3) 490 mJ    (4) 530 mJ

6. A force  $\vec{F} = (3x^2 + 2x - 7)\text{N}$  acts on a 2 kg body as a result of which the body gets displaced from  $x=0$  to  $x=5\text{m}$ . The work done by the force will be-

- (1) 35 J    (2) 70 J    (3) 115 J    (4) 270 J

7. A person of mass  $m$  is standing on one end of a plank of mass  $M$  and length  $L$  and floating in water. The person moves from one end to another and stops. Work done by normal force is -

- (1)  $MgL$     (2)  $mgL$     (3)  $\frac{mMgL}{M+m}$     (4) 0

8. A body of mass  $M$  tied to a string is lowered at a constant acceleration of  $(g/4)$  through a vertical distance  $h$ . The work done by the string will be.....

- (1)  $\frac{3}{4}Mgh$     (2)  $\frac{1}{4}Mgh$     (3)  $-\frac{3}{4}Mgh$     (4)  $-\frac{1}{4}Mgh$

9. A body of mass 6 kg under a force which causes displacement in it given ' $S = \frac{t^2}{4}$ ' metres where ' $t$ ' is time. The work done by the force in 2 seconds is :-

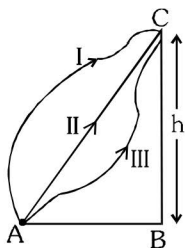
- (1) 12J    (2) 9J    (3) 6J    (4) 3J

10. A stone of mass  $m$  is tied to a string of length  $\ell$  at one end and by holding second end it is whirled into a horizontal circle, then work done will be :-

- (1) 0    (2)  $\left(\frac{mv^2}{\ell}\right)2\pi\ell$   
 (3)  $(mg)\cdot 2\pi\ell$     (4)  $\left(\frac{mv^2}{\ell}\right)\ell$

# WORK, POWER AND ENERGY

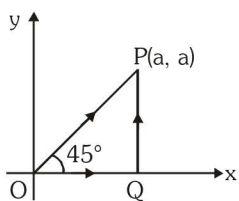
11. As shown in the diagram a particle is to be carried from point A to C via paths (I), (II) and (III) in gravitational field, then which of the following statements is correct :-



- (1) Work done is same for all the paths  
 (2) Work done is minimum for path (II)  
 (3) Work done is maximum for path (I)  
 (4) None of the above
12. A particle moves from a point  $(-4\hat{i} + 6\hat{j})$  to  $(5\hat{j} + 3\hat{k})$  when a force of  $(2\hat{i} + 3\hat{j})$  N is applied. How much work has been done by the force ?

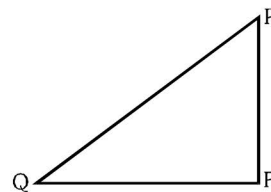
- (1) 5 J      (2) 2 J      (3) 8 J      (4) 11 J
13. The mass of a bucket full of water is 15 kg. It is being pulled up from a 15m deep well. Due to a hole in the bucket 6 kg water flows out of the bucket. The work done in drawing the bucket out of the well will be ( $g = 10\text{m/s}^2$ )-

- (1) 900 Joule      (2) 1500 Joule  
 (3) 1800 Joule      (4) 2100 Joule
14. A particle is moved from  $(0, 0)$  to  $(a, a)$  under a force  $\vec{F} = (3\hat{i} + 4\hat{j})$  from two paths. Path 1 is OP and path 2 is OQP. Let  $W_1$  and  $W_2$  be the work done by this force in these two paths. Then :

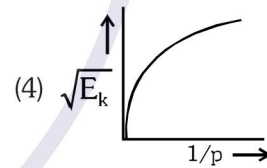
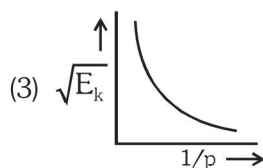
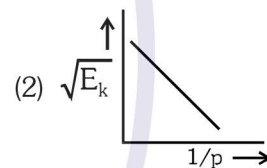
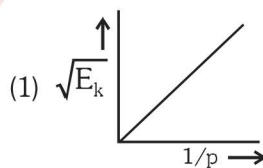


- (1)  $W_1 = W_2$       (2)  $W_1 = 2W_2$   
 (3)  $W_2 = 2W_1$       (4)  $W_2 = 4W_1$

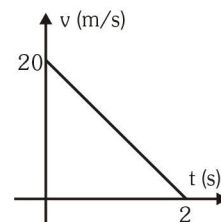
15. For the path PQR in a conservative force field the amounts work done in carrying a body from P to Q and from Q to R are 8 Joule and 2 Joule respectively. The work done in carrying the body from P to R will be -



- (1) 10 J      (2) 6 J      (3)  $\sqrt{68}$  J      (4) Zero
16. If K.E. increases by 4%. Then momentum will increase by :-
- (1) 1.5%      (2) 9%  
 (3) 3%      (4) 2%
17. The graph between  $\sqrt{E_k}$  and  $\frac{1}{p}$  is ( $E_k$  = kinetic energy and  $p$  = momentum) -



- (1)  $n$  times      (2)  $2n$  times  
 (3)  $\sqrt{n}$  times      (4)  $n^2$  times
18. If the momentum of a body is increased  $n$  times, its kinetic energy increases.
19. If K.E. body is increased by 100%. Then % change in 'P'.
- (1) 50%      (2) 41.4%      (3) 10%      (4) 20%
20. Velocity-time graph of a particle of mass 2 kg moving in a straight line is as shown in figure. Work done by all the forces on the particle is :

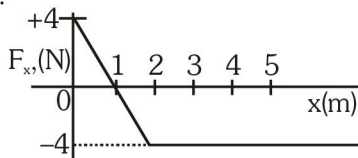


- (1) 400 J      (2) -400 J      (3) -200 J      (4) 200 J

# WORK, POWER AND ENERGY

- 21.** The only force  $F_x$  acting on a 2.0 kg body as it moves along the x-axis varies as shown in the figure. The velocity of the body along positive x-axis at  $x = 0$  is 4 m/s. The kinetic energy of the body at  $x = 3.0$  m is :-

- (1) 4 J  
(2) 8 J  
(3) 12 J  
(4) 16 J



- 22.** A uniform chain of length  $L$  and mass  $M$  is lying on a smooth table and  $\frac{2}{3}$  of its length is hanging down

over the edge of the table. If  $g$  is the acceleration due to gravity, the work done to pull the hanging part on the table is :-

- (1)  $MgL$       (2)  $\frac{MgL}{3}$       (3)  $\frac{MgL}{9}$       (4)  $\frac{2MgL}{9}$

- 23.** A particle in a certain conservative force field has a potential energy given by  $U = \frac{20xy}{z}$ . The force exerted on it is

- (1)  $\left(\frac{20y}{z}\right)\hat{i} + \left(\frac{20x}{z}\right)\hat{j} + \left(\frac{20xy}{z^2}\right)\hat{k}$   
 (2)  $-\left(\frac{20y}{z}\right)\hat{i} - \left(\frac{20x}{z}\right)\hat{j} + \left(\frac{20xy}{z^2}\right)\hat{k}$   
 (3)  $-\left(\frac{20y}{z}\right)\hat{i} - \left(\frac{20x}{z}\right)\hat{j} - \left(\frac{20xy}{z^2}\right)\hat{k}$   
 (4)  $\left(\frac{20y}{z}\right)\hat{i} + \left(\frac{20x}{z}\right)\hat{j} - \left(\frac{20xy}{z^2}\right)\hat{k}$

- 24.** If the potential energy of two molecules is give by,  $U = \frac{A}{r^{12}} - \frac{B}{r^6}$  then at equilibrium position, its potential energy is equal to :

- (1)  $\frac{A^2}{4B}$       (2)  $-\frac{B^2}{4A}$       (3)  $\frac{2B}{A}$       (4)  $3A$

- 25.** A 2 g ball of glass is released from the edge of a hemispherical cup whose radius is 20 cm. How much work is done on the ball by the gravitational force during the ball's motion to the bottom of the cup ?

- (1) 1.96 mJ  
(2) 3.92 mJ  
(3) 4.90 mJ  
(4) 5.88 mJ



- 26.** A body is dropped from a height  $h$ . When loss in its potential energy is  $U$  then its velocity is  $v$ . The mass of the body is -

- (1)  $\frac{U^2}{2v}$       (2)  $\frac{2v}{U}$       (3)  $\frac{2v}{U^2}$       (4)  $\frac{2U}{v^2}$

- 27.** A 0.5 kg ball is thrown up with an initial speed 14 m/s and reaches a maximum height of 8.0 m. How much energy is dissipated by air drag acting on the ball during the ascent ?

- (1) 19.6 joules      (2) 4.9 joules  
(3) 10 joules      (4) 9.8 joules

- 28.** A ball of mass 4 kg and another of mass 8 kg are dropped together from a 100 feet tall building. After a fall of 50 feet each towards earth, their respective kinetic energies will be in the ratio of:-

- (1) 1 : 4      (2) 1 : 2  
(3) 1 :  $\sqrt{2}$       (4)  $\sqrt{2}$  : 1

- 29.** A particle of mass  $m$  is moving in a horizontal circle of radius  $R$  under a centripetal force equal to  $-\frac{A}{r^2}$  ( $A = \text{constant}$ ). The total energy of the particle is :-

(Potential energy at very large distance is zero)

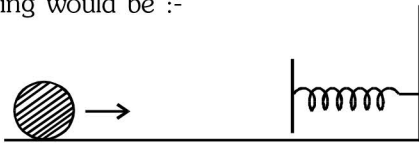
- (1)  $\frac{A}{R}$       (2)  $-\frac{A}{R}$       (3)  $\frac{A}{2R}$       (4)  $-\frac{A}{2R}$

- 30.** Consider a drop of rain water having mass 1 g falling from a height of 1 km. It hits the ground with a speed of 50 m/s. Take 'g' constant with a value  $10 \text{ m/s}^2$ . The work done by the (i) gravitational force and the (ii) resistive force of air is :-

- (1) (i) 1.25 J      (ii) - 8.25 J  
(2) (i) 100 J      (ii) 8.75 J  
(3) (i) 10 J      (ii) - 8.75 J  
(4) (i) - 10 J      (ii) - 8.25 J

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31. A mass of 0.5 kg moving with a speed of 1.5 m/s on a horizontal smooth surface, collides with a nearly weightless spring of force constant  $k=50\text{N/m}$ . The maximum compression of the spring would be :-



- (1) 0.12 m (2) 1.5 m  
 (3) 0.5 m (4) 0.15 m
32. A vertical spring with force constant  $k$  is fixed on a table. A ball of mass  $m$  at a height  $h$  above the free upper end of the spring falls vertically on the spring, so that the spring is compressed by a distance  $d$ . The net work done in the process is:

- (1)  $mg(h+d) + \frac{1}{2}kd^2$   
 (2)  $mg(h+d) - \frac{1}{2}kd^2$   
 (3)  $mg(h-d) - \frac{1}{2}kd^2$   
 (4)  $mg(h-d) + \frac{1}{2}kd^2$

33. A block of mass  $M$  is attached to the lower end of a vertical spring. The spring is hung from a ceiling and has force constant value  $k$ . The mass is released from rest with the spring initially unstretched. The maximum extension produced in the length of the spring will be :-

- (1)  $Mg/2k$  (2)  $Mg/k$   
 (3)  $2 Mg/k$  (4)  $4 Mg/k$

34. If a spring extends by  $x$  on loading then energy stored by the spring is :- ( $T$  is tension in the spring,  $K$  = spring const.)

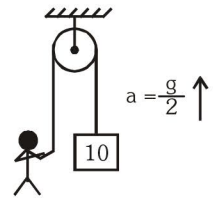
- (1)  $\frac{T^2}{2x}$  (2)  $\frac{T^2}{2k}$  (3)  $\frac{2k}{T^2}$  (4)  $\frac{2T^2}{k}$

35. Two men with weights in the ratio 2 : 3 run up a staircase in times in the ratio 10 : 7. The ratio of power of first to that of second is -

- (1)  $\frac{7}{15}$  (2)  $\frac{15}{7}$  (3)  $\frac{10}{7}$  (4)  $\frac{7}{10}$

36. Calculate power generated by tension in the string in first 4 seconds of motion :-

- (1) 250 W  
 (2) 750 W  
 (3) 1500 W  
 (4) 1000 W



37. A body of mass  $m$  starting from rest from origin moves along  $x$ -axis with constant power ( $P$ ). Calculate relation between velocity and distance :-

- (1)  $x \propto v^{1/2}$  (2)  $x \propto v^2$   
 (3)  $x \propto v$  (4)  $x \propto v^3$

38. A pump is used to deliver water at a certain rate from a given pipe. To obtain  $n$  times water from the same pipe in the same time, by what factor, the force of the motor should be increased?

- (1)  $n$  times (2)  $n^2$  times  
 (3)  $n^3$  times (4)  $\frac{1}{n}$  times

39. Water is falling on the blades of a turbine at a rate of 100 kg/s from a certain spring. If the height of the spring be 100 metres, the power transferred to the turbine will be :-

- (1) 100 kW (2) 10 kW  
 (3) 1 kW (4) 1000 kW

40. A constant force  $\vec{F}$  is acting on a body of mass  $m$  with constant velocity  $\vec{v}$  as shown in the figure. The power  $P$  exerted is



- (1)  $Fv \cos\theta$  (2)  $\frac{F \cos\theta}{mg}$   
 (3)  $\frac{Fmg \cos\theta}{v}$  (4)  $\frac{mg \sin\theta}{F}$

41. An engine pumps water continuously through a hose. Water leaves the hose with a velocity  $v$  and  $m$  is the mass per unit length of the water jet. What is the rate at which kinetic energy is imparted to water :-

- (1)  $\frac{1}{2} m^2v^2$  (2)  $\frac{1}{2} mv^3$   
 (3)  $mv^3$  (4)  $\frac{1}{2} mv^2$

# WORK, POWER AND ENERGY

- 42.** A particle of mass  $m$  is driven by a machine that delivers a constant power  $k$  watts. If the particle starts from rest the force on the particle at time  $t$  is :-
- (1)  $\sqrt{mk} t^{-1/2}$                       (2)  $\sqrt{2mk} t^{-1/2}$   
 (3)  $\frac{1}{2}\sqrt{mk} t^{-1/2}$                       (4)  $\sqrt{\frac{mk}{2}} t^{-1/2}$
- 43.** A body of mass  $m$  accelerates uniformly from rest to  $v_1$  in time  $t_1$ . The instantaneous power delivered to the body as a function of time  $t$  is-
- (1)  $\frac{mv_1 t}{t_1}$     (2)  $\frac{mv_1^2 t}{t_1^2}$     (3)  $\frac{mv_1 t^2}{t_1}$     (4)  $\frac{mv_1^2 t}{t_1}$
- 44.** A body of mass  $4$  kg is moving up an inclined plane rising  $1$  in  $40$  with velocity  $40$  m/sec if efficiency is  $50\%$  the calculate power required.
- (1)  $38.4$  W                      (2)  $55$  W  
 (3)  $78.4$  W                      (4)  $108$  W
- 45.** A  $1.0$  hp motor pumps out water from a well of depth  $20$  m and fills a water tank of volume  $2238$  liters at a height of  $10$  m from the ground. The running time of the motor to fill the empty water tank is ( $g = 10\text{ms}^{-2}$ )
- (1)  $5$  minutes                      (2)  $10$  minutes  
 (3)  $15$  minutes                      (4)  $20$  minutes
- 46.** Work done in time  $t$  on a body of mass  $m$  which is accelerated from rest to a speed  $v$  in time  $t_1$  as a function of time  $t$  is given by :-
- (1)  $\frac{1}{2}m\frac{v}{t_1}t^2$                       (2)  $m\frac{v}{t_1}t^2$   
 (3)  $\frac{1}{2}\left(\frac{mv}{t_1}\right)^2 t^2$                       (4)  $\frac{1}{2}m\frac{v^2}{t_1^2}t^2$
- 47.** A car of mass  $m$  starts from rest and accelerates so that the instantaneous power delivered to the car has a constant magnitude  $P_0$ . The instantaneous acceleration of this car is proportional to :-
- (1)  $t^{1/2}$                       (2)  $t/\sqrt{m}$   
 (3)  $t^2P_0$                       (4)  $t^{-1/2}$
- 48.** The heart of a man pumps  $10$  litres of blood through the arteries per minute at a pressure of  $75$  mm of mercury. If the density of mercury be  $13.6 \times 10^3 \text{kg/m}^3$  and  $g = 10\text{m/s}^2$  then the power of heart in watt is:
- (1)  $1.50$     (2)  $1.70$     (3)  $2.35$     (4)  $3.0$
- 49.** A body of mass  $1$  kg begins to move under the action of a time dependent force  $\vec{F} = (2t\hat{i} + 3t^2\hat{j})\text{N}$ , where  $\hat{i}$  and  $\hat{j}$  are unit vectors along  $x$  and  $y$  axis. What power will be developed by the force at the time  $t$  ?
- (1)  $(2t^2 + 3t^3)\text{W}$                       (2)  $(2t^2 + 4t^4)\text{W}$   
 (3)  $(2t^3 + 3t^4)\text{W}$                       (4)  $(2t^3 + 3t^5)\text{W}$

## ANSWER KEY

|      |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Que. | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
| Ans. | 3  | 2  | 2  | 3  | 1  | 3  | 4  | 3  | 4  | 1  | 1  | 1  | 3  | 1  | 1  |
| Que. | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| Ans. | 4  | 3  | 4  | 2  | 2  | 3  | 4  | 2  | 2  | 2  | 4  | 4  | 2  | 4  | 3  |
| Que. | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 |
| Ans. | 4  | 2  | 3  | 2  | 1  | 3  | 4  | 2  | 1  | 1  | 2  | 4  | 2  | 3  | 3  |
| Que. | 46 | 47 | 48 | 49 |    |    |    |    |    |    |    |    |    |    |    |
| Ans. | 4  | 4  | 2  | 4  |    |    |    |    |    |    |    |    |    |    |    |