

TRIGONOMETRIC RATIO - EXERCISE

1. If ABCD is a cyclic quadrilateral such that $12 \tan A - 5 = 0$ and $5 \cos B + 3 = 0$ then the quadratic equation whose roots are $\cos C$, and $\tan D$ is-
- (1) $39x^2 - 16x - 48 = 0$
 - (2) $39x^2 + 88x + 48 = 0$
 - (3) $39x^2 - 88x + 48 = 0$
 - (4) None of these
2. $\cos(\alpha + \beta) = \frac{1}{e}$, $\cos(\alpha - \beta) = 1$ find no. of ordered pair of (α, β) , $-\pi \leq \alpha, \beta < \pi$
- (1) 0
 - (2) 1
 - (3) 2
 - (4) 4
3. If θ & ϕ are acute angles such that $\sin \theta = \frac{1}{2}$ and $\cos \phi = \frac{1}{3}$ then $\theta + \phi$ lies in-
- (1) $\left(\frac{\pi}{3}, \frac{\pi}{2}\right]$
 - (2) $\left(\frac{\pi}{2}, \frac{2\pi}{3}\right]$
 - (3) $\left(\frac{2\pi}{3}, \frac{5\pi}{6}\right]$
 - (4) $\left(\frac{\pi}{6}, \pi\right]$
4. The value of $\cos \frac{2\pi}{7} + \cos \frac{4\pi}{7} + \cos \frac{6\pi}{7} + \cos \frac{7\pi}{7}$ is-
- (1) 1
 - (2) -1
 - (3) $1/2$
 - (4) $-3/2$
5. If $\cot \alpha$ equals the integral solution of the inequality $4x^2 - 16x + 15 < 0$ and $\sin \beta$ equals to the slope of the bisector of the first quadrant, then $\sin(\alpha + \beta) \sin(\alpha - \beta)$ is equal to-
- (1) $-3/5$
 - (2) $-4/5$
 - (3) $2/\sqrt{5}$
 - (4) 3
6. If $\sin x + \cos x = a$, $a \in [-\sqrt{2}, \sqrt{2}] - \{-1, 1\}$, then $\sum_{n=1}^{\infty} (\sin^n x + \cos^n x)$ is equal to -
- (1) $\frac{2(1+a-a^2)}{(a+1)^2}$
 - (2) $\frac{2(a^2-a+1)}{(a-1)^2}$
 - (3) $\frac{2(a^2-a+1)}{(a+1)^2}$
 - (4) $\frac{2(1+a-a^2)}{(a-1)^2}$
7. If $\frac{\sec 8\theta - 1}{\sec 4\theta - 1} = \frac{a + b \tan^2 2\theta}{1 + c \tan^2 2\theta + d \tan^4 2\theta}$ (where $\theta \neq \frac{n\pi}{16}$, $n \in \mathbb{I}$), then value of $(a - b + c - d)$ is -
- (1) 0
 - (2) 1
 - (3) 7
 - (4) 13
8. If $\alpha, \beta, \gamma, \delta$ are the smallest positive angles in ascending order of magnitude which have their sines equal to the positive quantity k , then the value of $4\sin \frac{\alpha}{2} + 3\sin \frac{\beta}{2} + 2\sin \frac{\gamma}{2} + \sin \frac{\delta}{2}$ is equal to :-
- (1) $2\sqrt{1-k}$
 - (2) $\frac{1}{2}\sqrt{1+k}$
 - (3) $2\sqrt{1+k}$
 - (4) None of these
9. The sum of the maximum and minimum values of the function $f(x) = \frac{1}{1 + (2\cos x - 4\sin x)^2}$ is :-
- (1) $\frac{22}{21}$
 - (2) $\frac{21}{20}$
 - (3) $\frac{22}{20}$
 - (4) $\frac{21}{11}$
10. In ΔABC $\sin^2 A + \sin^2 B + \sin^2 C = 2$ then triangle is :-
- (1) Equilateral
 - (2) Right angle
 - (3) Isosceles
 - (4) None
11. The value of expression $\frac{2(\sin 1^\circ + \sin 2^\circ + \sin 3^\circ + \dots + \sin 89^\circ)}{2(\cos 1^\circ + \cos 2^\circ + \dots + \cos 44^\circ) + 1}$ equals:-
- (1) $\sqrt{2}$
 - (2) $1/\sqrt{2}$
 - (3) $1/2$
 - (4) 0
12. Let $x = \sin 1^\circ$, then the value of the expression :- $\frac{1}{\cos 0^\circ \cdot \cos 1^\circ} + \frac{1}{\cos 1^\circ \cdot \cos 2^\circ} + \frac{1}{\cos 2^\circ \cdot \cos 3^\circ} + \dots + \frac{1}{\cos 44^\circ \cdot \cos 45^\circ}$ is equal to
- (1) x
 - (2) $1/x$
 - (3) $\sqrt{2}/x$
 - (4) $x/\sqrt{2}$

13. Value of $\frac{3 + \cot 80^\circ \cot 20^\circ}{\cot 80^\circ + \cot 20^\circ}$ is equal to :-
 (1) $\cot 20^\circ$ (2) $\tan 50^\circ$
 (3) $\cot 50^\circ$ (4) $\cot \sqrt{20^\circ}$
14. The value of :-
 $\sin \frac{\pi}{14} \sin \frac{3\pi}{14} \sin \frac{5\pi}{14} \sin \frac{7\pi}{14} \sin \frac{9\pi}{14} \sin \frac{11\pi}{14} \sin \frac{13\pi}{14}$ is equal to
 (1) $\frac{1}{8}$ (2) $\frac{1}{16}$ (3) $\frac{1}{32}$ (4) $\frac{1}{64}$
15. The value of $\sin^2 5^\circ + \sin^2 10^\circ + \sin^2 15^\circ + \dots + \sin^2 85^\circ$ is equal to :-
 (1) 7 (2) $8\frac{1}{2}$ (3) 9 (4) $9\frac{1}{2}$
16. $\tan \alpha + 2 \tan 2\alpha + 4 \tan 4\alpha + 8 \cot 8\alpha$:-
 (1) $\tan \alpha$ (2) $\tan 2\alpha$ (3) $\cot \alpha$ (4) $\cot 2\alpha$
17. $\sin^4 \frac{\pi}{8} + \sin^4 \frac{3\pi}{8} + \sin^4 \frac{5\pi}{8} + \sin^4 \frac{7\pi}{8} =$
 (1) $\frac{1}{2}$ (2) $\frac{1}{4}$ (3) $\frac{3}{2}$ (4) $\frac{3}{4}$
18. The maximum value of the expression $\frac{1}{\sin^2 \theta + 3 \sin \theta \cos \theta + 5 \cos^2 \theta}$ is
 (1) 2 (2) $\frac{1}{2}$
 (3) 1 (4) None of these
19. If $\sin x + \sin^2 x + \sin^3 x = 1$, then $\cos^6 x - 4 \cos^4 x + 8 \cos^2 x =$:-
 (1) 3 (2) 4 (3) 2 (4) 1
20. If α is the common positive root of the equation $x^2 - ax + 12 = 0$, $x^2 - bx + 15 = 0$ and $x^2 - (a+b)x + 36 = 0$ and $\cos x + \cos 2x + \cos 3x = \alpha$, then $\sin x + \sin 2x + \sin 3x =$
 (1) 3 (2) -3
 (3) 0 (4) none of these

21. If $\cos \alpha + \cos \beta = a$, $\sin \alpha + \sin \beta = b$, then $\cos(\alpha + \beta)$ is equal to :-
 (1) $\frac{2ab}{a^2 + b^2}$ (2) $\frac{a^2 + b^2}{a^2 - b^2}$
 (3) $\frac{a^2 - b^2}{a^2 + b^2}$ (4) $\frac{b^2 - a^2}{b^2 + a^2}$
22. Which of the following is correct :-
 (1) $\sin 1 > \sin 2 > \sin 3$ (2) $\sin 1 < \sin 2 < \sin 3$
 (3) $\sin 1 < \sin 3 < \sin 2$ (4) $\sin 3 < \sin 1 < \sin 2$
23. The maximum value of $12 \sin \theta - 9 \sin^2 \theta$ is :-
 (1) 3 (2) 4
 (3) 5 (4) None of these
24. If $y = 9 \sec^2 x + 16 \operatorname{cosec}^2 x$, find the minimum value of y for all permissible value of x .
 (1) 49 (2) 50 (3) 24 (4) 25
25. $\log(\sin 1^\circ) \log(\sin 2^\circ) \log(\sin 3^\circ) \dots \dots \log(\sin 179^\circ)$ is equal to -
 (1) 1 (2) 0 (3) 2 (4) -1
26. If $A = \sin 45^\circ + \cos 45^\circ$ and $B = \sin 44^\circ + \cos 44^\circ$, then:-
 (1) $A > B$ (2) $A < B$
 (3) $A = B$ (4) None of these
27. If in a ΔABC , $\angle C = 90^\circ$, then the maximum value of $\sin A \sin B$ is -
 (1) $\frac{1}{2}$ (2) 1
 (3) 2 (4) None of these
28. If $\tan x + \tan y = 25$ and $\cot x + \cot y = 30$, then the value of $\tan(x + y)$ is
 (1) 150 (2) 200 (3) 250 (4) 100
29. If the maximum value of $y = \frac{7 + 6 \tan x - \tan^2 x}{(1 + \tan^2 x)}$ is λ then the value of $\log_{\sqrt{2}}(\lambda)$ is
 (1) 0 (2) 6
 (3) 8 (4) 1
30. If $0 < \theta < \pi$, then minimum value of $3 \sin \theta + \operatorname{cosec}^3 \theta$ is :-
 (1) 4 (2) 3 (3) 5 (4) 6

ANSWER KEY

Exercise-I

Que.	1	2	3	4	5	6	7	8	9	10
Ans.	1	4	2	4	2	4	2	3	1	2
Que.	11	12	13	14	15	16	17	18	19	20
Ans.	1	2	2	4	2	3	3	1	2	3
Que.	21	22	23	24	25	26	27	28	29	30
Ans.	3	4	2	1	2	1	1	1	2	1